

## Safety and Reliability of Embedded Systems

### (Sicherheit und Zuverlässigkeit eingebetteter Systeme)

#### Fault Tree Analysis

#### Current Research Issues

## Content

- Current Research Issues
- Original Contributions from Researchers
  - Prof. John Andrews, Loughborough University, United Kingdom
  - Prof. Joanne Bechta Dugan, University of Virginia, USA
  - Prof. Janusz Górska, Gdańsk University of Technology, Poland
  - Dr. Bernhard Kaiser, formerly Fraunhofer IESE, Germany
  - Prof. Antoine Rauzy, Institut de Mathématiques de Luminy, France
  - Prof. Anders Ravn, Aalborg University, Denmark
  - Prof. Wolfgang Reif, Universität Augsburg, Germany
  - Prof. Kishor Trivedi, Duke University, USA

... show their view on fault trees and their research approaches

## Current Research Issues

- Formalization and Extension of Fault Trees
  - Formal semantics of FTs, events and gates
  - Checking FTs for completeness and consistency
  - Temporal order and real time
  - Multistate components
- Analysis Techniques
  - Performance, accuracy and usability issues with BDDs
  - Other techniques (Markov, Petri Net...) where BDD is not applicable
- Integration with Other Techniques
  - Automatic FTA generation from SW/HW documents
  - Integration with other safety analysis techniques
  - Integration with formal methods
  - Integration into a development / safety analysis process

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## Fault Tree Analysis - Methodology

- Increasing the FTA efficiency / accuracy
  - Analysis by BDD
    - Procedures to permit all qualitative and quantitative analysis currently performed by conventional FTA methods to be performed utilising the inherent efficiency and accuracy of the BDD
    - Development of efficient BDD construction methods
      - Variable ordering schemes / direct FT gate transformation
  - Non-coherent fault tree analysis
    - Extension of analysis methods for this type of assessment (useful for Event Tree Analysis)
    - Development of appropriate component importance measures to account for the contribution to the system failure of both failed and functioning component states
  - Automatic generation of the fault tree from the system schematic

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## Fault Tree Analysis - Applications

- Increasing the range of applications of the FTA method
  - System Reliability Analysis
    - Phased Mission
      - A mission made up of several consecutive phases all of which must be successful for mission success (repairable and non-repairable)
    - Dependency Modelling
      - Integrate FTA with Markov and simulation modelling techniques to handle dependencies (such as the time limited dispatch of commercial aircraft – the aircraft is permitted to take off carrying known faults for a limited period of time)
    - Optimisation
      - Embedding the system analysis within an optimisation process (usually a genetic algorithm) to yield the best rather than adequate level of performance within the limitations placed on the resources available

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## Fault Tree Analysis – Other Uses

- Increasing the range of applications of the FTA method
  - Systems Diagnostics and Prognostics
    - System Diagnostics
      - Use fault trees which develop causes of sensor deviations to determine if component faults exist on a system and if so what they are
    - System Prognostics
      - Integrated with the fault diagnostics approach, it is used to determine the likelihood of a mission success when faults occur. When an unacceptable likelihood is predicted the mission or the system can be reconfigured (applications such as UAVs – unmanned air vehicles)

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## Dynamic Fault Tree Analysis

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## DFT: Dynamic Fault Tree Analysis

- Fault tree analysis (FTA) is a widely accepted methodology for reliability analysis and provides core functionality to PRA (Probabilistic Risk Assessment)
- However, FTA cannot model failure events that depend on the order in which components fail
- Dynamic fault trees (DFT) extend FTA to allow accurate analysis of computer-based systems characterized by
  - complex redundancy management
  - spares (cold, warm, pooled)
  - functional and sequence dependencies
  - hardware and software components
  - imperfect coverage and other common cause failures
  - phased missions

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## DFT: Dynamic Fault Tree Analysis

- The DFT methodology supports modularization
  - Overall DFT model is **automatically** divided into modules that can be solved separately
  - Modules are classified as static (containing traditional gates) or dynamic (containing at least one dynamic gate)
  - Separate modules are solved using most appropriate means and results are synthesized **automatically**

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## Static Fault Trees

- Combinatorial model (models combinations of events)
  - AND gates
  - OR gates
  - K-of-M gates
- New approach for solution: BDD (Binary Decision Diagrams)
- Advantages
  - Exact analysis without cutsets
  - Can include repeated events
  - Can include coverage modeling
  - Fast solution for very large models
- Disadvantage
  - Static model: cannot include sequence dependencies

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## Dynamic Fault Trees

- Include special constructs for modeling sequence dependencies
  - functional dependencies
  - hot, warm and cold spares
  - priority-AND
  - sequence enforcing
- Solution: convert to Markov chain
- Advantages
  - easier to use fault tree than Markov model directly
  - can model dynamic redundancy, shared pools of spares, etc
- Disadvantage
  - state space explosion -- worst case exponential in number of basic events

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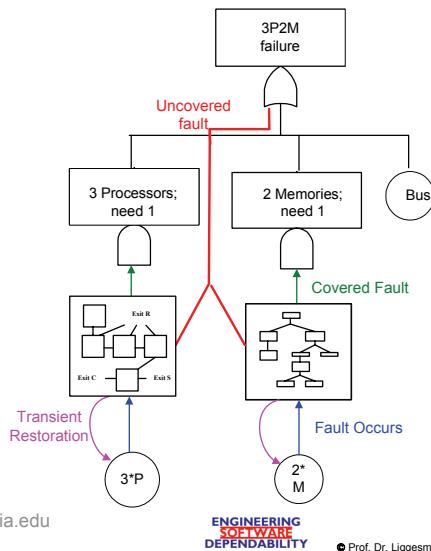
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## Coverage Modeling

- Adaptive (computer-based) systems can exhibit multiple failure modes
- Covered** (benign) failure can be handled automatically
  - error is detected and located
  - switch in spare or bypass faulty component
  - system can continue operation without manual intervention
- Uncovered** failure is globally malicious
  - undetected error escapes from embedded system
  - faulted component cannot be disabled
  - malicious behavior confuses recovery procedures
- System dependability measures are very sensitive to coverage
- Good techniques exist for incorporating coverage into static and dynamic fault trees



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## Unique Features in our\* DFT Methodology

- Modularization allows solution of large systems
- Combines Markov analysis with BDD analysis automatically
- Automatic generation of Markov model or BDD
- Coverage modeling for computer-based systems
- Common cause failure analysis is modeled implicitly (efficiently)
- Sensitivity analysis for static and dynamic models

\*Joint work with Kevin Sullivan, Dept. Computer Science, University of Virginia and David Coppit, Dept Computer Science, The College of William & Mary.

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## Unique Features in our\* DFT Methodology

- Phased mission analysis for both static & dynamic models
- Exact results (no hidden approximations)
- Uncertainty analysis for both static & dynamic trees
- Diagnostic support to help determine cause of failure given symptoms and partial information
- DFT model has been formally specified\* (i.e. in Zed) to ensure that subtle interactions between gates are handled properly

\*Joint work with Kevin Sullivan, Dept. Computer Science, University of Virginia and David Coppit, Dept Computer Science, The College of William & Mary.

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## FTA Formalization and analysis of timing properties

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## Approach: event structures and duration calculus

### Initiation of the research

- Górski J: *Towards a common formal semantics base for safety description model*. EUREKA Project SEW 263, Rep. SDM/JG/01, 1990.
- Górski J: *Interfacing fault trees to formal methods*. EUREKA Project SEW 263, Rep. SDM/JG/03, 1990.

### Continuation of the research - Publications

- Bloomfield R.E., Chang J. H., Górski J.: *Towards a Common Safety Description Model*. Proc. SAFECOMP'91, (J.F. Lindeberg, Ed.), Pergamon Press, 1991, pp. 1-6
- Górski J., *Extending Safety Analysis techniques with Formal Semantics*, in *Technology and Assessment of Safety-Critical Systems* (F.J. Redmill and T. Anderson, eds.), Springer-Verlag, 1994, pp. 147-163
- Górski, J. and Wardziński, A., *Formalizing Fault Trees*, Safety Critical Systems Symposium, Brighton (UK), February 1995, Springer Verlag, 1994, pp. 311-327
- Górski, J. and A. Wardziński, *Formalizing Fault Trees*, in *Achievement and Assurance of Safety*, (F Redmill and T Anderson, eds.), Springer Verlag, 1995, pp. 311-327
- Górski, J., and A. Wardziński, *Deriving Real-Time Requirements for Software from Safety Analysis*, 8th EUROMICRO Workshop on Real-Time Systems, L'Aquila (Italy), June 12-14, 1996, IEEE Press, 1996, pp. 9-14
- Górski, J. and Wardzinski, A., *Timing Aspects of Safety Analysis*, in *Safer Systems*, (F Redmill and T Anderson Eds.), Springer Verlag, 1997, pp. 231-244

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## Approach: event structures and duration calculus

### Doctoral Dissertation

- Andrzej Wardziński, *Fault Tree Analysis of Safety Related Computer Systems* (in Polish), Faculty of Electronics, Telecommunications and Informatics, Gdańsk University of Technologies, 1997 (Supervisor: Prof. Janusz Górski)

### Master Dissertations

- Jarmuż Piotr, *Safety analysis of real time computer systems* (in Polish), Franco-Polish School of New Information and Communication Technologies , 1996 (Supervisor: prof. J. Górski)
- Grzegorz Golaszewski, *A tool supporting Fault Tree Analysis of real time requirements* (in Polish), Faculty of Electronics, Telecommunications and Informatics, Gdańsk University of Technologies, 2004 (Supervisor: Prof. Janusz Górski)

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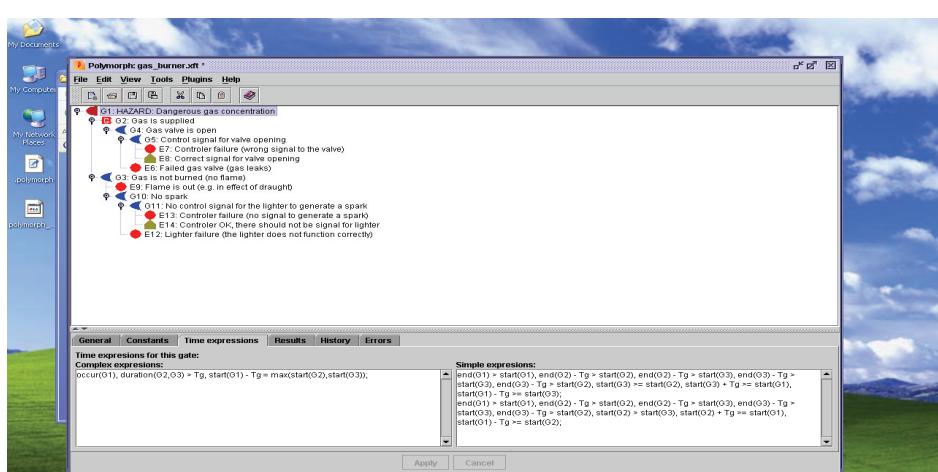
## Approach: Petri Net modeling

- Górski J., Magott J. and Wardziński A., *Modelling Fault Trees Using Timed Petri Nets* (G Rabe, ed.), Springer Verlag, 1995, pp. 90-100
- Magott J. Skrobanek P, *A method of analysis of fault trees with time dependencies*, (Koornneef F and van der Meulen M eds) Springer-Verlag, 2000, 382-394
- J Magott, P Skrobanek, *Method of time Petri net analysis for analysis of fault trees with time dependencies*, IEE Proc. . Computers and Digital Techniques vol 149 no 6, 2002

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The tool POLYMORPH-FTA  
 supporting time analysis of Fault Trees  
*Prototype version of the tool will be available by the end of 2004*

The Gas Burner case study

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## Extending FTA for software-controlled systems: Component Fault Trees, State-Event-Fault-Trees



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## Problems Addressed

- Many Embedded Systems go into Safety Critical Areas  
→ Safety and Reliability Analysis (e.g. by Fault Tree Analysis) is required
- Need for Compositional Techniques
  - ! Models must be attached to Components defined during Design
  - ! Component models need interfaces that allow integration

⌚ Traditional FT Modularisation only for *Independent Subtrees*

😊 New Component Fault Tree Concept allows Input and Output Ports

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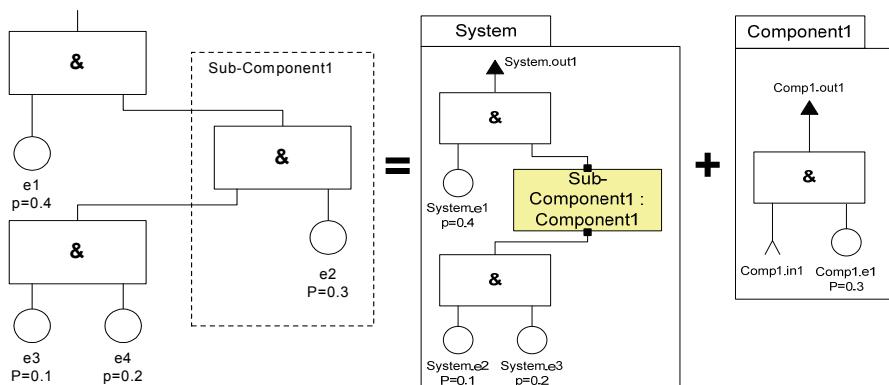
## Problems Addressed

- Software-Controlled Systems require Adequate Models
  - ! Capture Software Behaviour (States, Sequences of Actions)
  - ! Model Multi-State Components
  - ! Integrate with Software Design Models
  - ⌚ Traditional FTA is a Combinatorial Model (only Boolean Logic)
  - ⌚ State-Event-Fault-Trees are a State-Based Model distinguishing states and events and allowing temporal propositions in an intuitive notation

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## Component Fault Trees

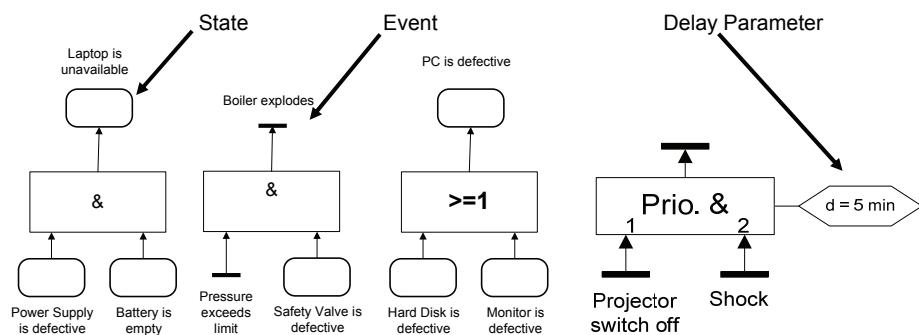


**Components are actual technical units, joint by ports.  
Components represent Boolean formulas, not probabilities!**

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## State-Event-Fault-Trees



Informally: Combination of Fault Trees and Statecharts

- State/Event Consistency is checked
- Unambiguous Semantics
- Analysis by Translation into Petri Nets

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## The UWG3 / ESSaRel Tool Project

- Windows based GUI Tools under .NET
  - Intuitive Use (Drag&Drop, Project Explorer...)
  - XML File-Format for Collaboration and Reuse
- UWG3
  - Supports Component Fault Trees
  - Collaboration with Siemens
  - First Version in 2003
  - Successful Evaluation in Industry Projects
- ESSaRel
  - Embedded Systems Safety and Reliability Analyser
  - Available Spring 2005
  - SEFTs, Markov Chains, State Diagrams
  - Analysis by Translation to Petri Nets (DSPNs)
  - Interfaces to Rational Rose RT and TimeNET
- Download at [www.essarel.de](http://www.essarel.de)

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## Semi-automatic synthesis of Fault Trees

- Inputs to the synthesis algorithm
  - A. Topological model of the system that identifies components and material, energy and data transactions among those components
  - B. Logical expressions that, for each component, determine how **deviations of component outputs** are caused by **internal malfunctions** or **deviations of component inputs**  
In this type of failure logic, input and output deviations are described qualitatively representing conditions such as the omission or commission of parameters and deviations from correct value (i.e. hi-low) or expected timing behaviour (i.e. early-late)
- Fault Tree Synthesis Algorithm: Combines a backward traversal of the model and evaluation of failure expressions encountered in the course of the traversal

## Semi-automatic synthesis of Fault Trees

Output of the synthesis algorithm

A network of interconnected fault trees which show how component failures combine and propagate through the model to cause hazardous failures at system outputs

Fault trees currently incorporate only classical AND & OR gates. However, the aim is to extend this logic with NOT and temporal gates (i.e. "Priority AND" or "AND THEN" gates)

Synthesis tool operates on **Matlab Simulink** and **Simulation X** models. It has its own fault tree analysis capabilities, but also interfaces with **FT+** a commercial fault tree analysis tool (by **Isograph Ltd**). The tool is experimental but usable by third parties

Case studies have been reported on complex prototypes in conjunction with **DaimlerChrysler**, **Volvo Cars** and **Germanisher Lloyd**

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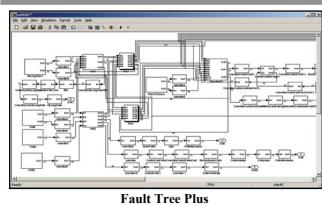
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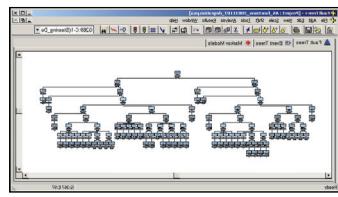
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## Semi-automatic synthesis of Fault Trees



Simulink model and fault tree of a steer-by-wire prototype by Volvo



### OTHER RELATED WORK BY THE SAME GROUP

1. **Automatic Analysis:** Synthesis of FMEAs
2. **Automated Monitoring:** Diagnosis & correction of failures using a combination of state-charts and fault trees as an executable monitoring model
3. Optimisation of system designs (combining genetic algorithms and fault tree synthesis)
  - **Optimal allocation of redundancies**
  - **Optimal allocation of reliability requirements on components of evolving architectures**

Further info @ [www2.dcs.hull.ac.uk/people/cssyp](http://www2.dcs.hull.ac.uk/people/cssyp)

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## Can We Trust Fault Trees / Event Trees Analyses?

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## Current situation in the (nuclear, avionic, ...) industry

- Models (fault trees/event trees) are
  - Huge (several thousands gates and basic events)
  - Highly tool-dependant
  - therefore ...
  - Difficult to master (size)
  - Impossible to redesign (economical reasons)
  
- Assessment tools are
  - Very efficient and user friendly
  - but ...
  - Based on the same technology (minimal cutsets) that relies on approximations (rare events, cut-offs, *ad-hoc* treatment of success branches)

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## Problems and Perspectives

### Known problems

- Most part of models is useless (in general, more than 90% of the basic events never show up in cutsets)
- Accuracy of results is unpredictable (approximations)
- Cross verifications of results with different tools is hard (tool-dependency) and useless (same underlying technology)

### Hot research topics

- Design of a sound mathematical framework (non coherent models, importance factors, ...)
- Improvement the BDD technology to make it able to deal with (all, most of the) large models of the industry
- Automated model refactoring

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## Fault Trees in Safety Analysis

- A fault tree is a formula in a logic used for analysing safety
- The formula is constructed by backwards reachability analysis from a primary fault - a top event
- The formula is a "counterexample" to the system being safe
- The safety requirement is formally the negation of the formula

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## Fault Tree Semantics

- Safety analysis is concerned with dynamical systems (state changing with time)
  - Special case: programs (transition systems) in general hybrid systems
- The model for the logic must thus include both state and time, and the formula must be able to specify both temporal and state dependent properties
- Intermediate nodes must be names of formulas, elementary nodes must denote properties of the dynamical system, combined using the logical connectives

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## Fault Tree Semantics

- The safety requirement corresponding to a top event E is **NOT  $\leftrightarrow$  E** (not somewhere E) or equivalently  $\Box \text{NOT } E$  (invariantly NOT E). E is itself a composite formula
  - Note in particular, that in modal logics  $\leftrightarrow(A \text{ AND } B)$  is much stronger than  $\leftrightarrow A \text{ AND } \leftrightarrow B$
- That is the rationale for looking for "cut sets" where one assumes simultaneous occurrence
- If one wants complications, one can use (semi)Markov processes as model

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## Fault Trees as Software Requirements

- The dynamical system model of the safety analysis is represented by an observed state in embedded software
- The algorithms in embedded software manipulate this representation of the state and produces inputs and outputs
- The invariants should be maintained by the algorithms
- Could e.g. be model checked

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## Formal FTA

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- Formal semantics in interval temporal logic (ITL)
  - Each gate is represented by an ITL-formula
- Features
  - Events may have durations
  - Distinction between synchronous causes and asynchronous causes
  - Causes must happen before consequences (better than Hansen semantics)
- Formally proven: minimal cut set theorem

## Minimal cut set theorem

- Minimal cut sets of ITL semantics preserve intuitive understanding
- Theorem: if all gates have been verified, than prevention of one element of every minimal cut set prevents the hazard (i.e. no branches have been forgotten in the fault tree)

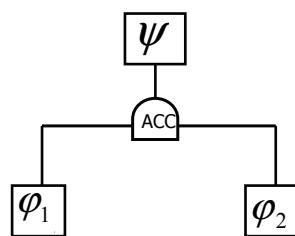
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## Example

- Asynchronous cause-consequence gate
  - Informal: Both  $\varphi_1$  and  $\varphi_2$  must happen before  $\psi$ , but not necessarily simultaneously
- Verification condition
  - Informal: „There exists no trace in the system, such that  $\psi$  occurs without previous appearance of  $\varphi_1$  and  $\varphi_2$ “



ITL-operators

$$\neg(\neg\lozenge\varphi_1 \wedge \neg\lozenge\varphi_2; \psi)$$

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## Summary: FTA Semantics

- 7 different types of gates for describing precise fault trees, including
  - AND-, OR-gates with Boolean semantics
  - AND-, OR-gates with cause-consequence relationship
  - Distinction Synchronous/Asynchronous
  - INHIBIT-gates

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## Tool Support

- For infinite state models
  - interactive theorem prover KIV (supports fault trees, state charts, ITL)
- For finite state models
  - Automatic model checking with SMV in CTL (only possible for events without duration)
- Integrated in formal safety analysis approach
  - ForMoSA approach (includes formal verification, analysis of failure modes, formal FTA, formal FMEA and quantitative risk optimizations)

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## FTA Contributions from Trivedi's Group

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## FTA Contributions

- Better understanding of FTA
  - Compare modeling powers of various dependability models [mal94]
  - Survey of SDP method in FTA [rai95]
- Extension of FTA
  - Use FTA for phased-mission systems [ma99, zang99]
  - Use FTA for multistate systems [vee94, zang03]
  - Reliability analysis using FT for repairable systems [bal95]
- New algorithms for FTA
  - SDP based [luo98]
  - BDD based [zang99, zst99, zang03]
- Combining FTA with other modeling techniques
  - Hierarchical modeling [bbook, rbook]
  - Relation between FT and Petri nets [mal95]

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## FTA in SHARPE

- SHARPE software package [sha]
- Symbolic Hierarchical Automated Reliability and Performance Evaluator
- Supported model types using FTA technique
  - Reliability Block Diagrams
  - Fault trees with repeated events
  - Reliability Graphs
  - Phased-mission Systems
  - Multi-state Fault Trees
- FTA techniques in SHARPE
  - Factoring, SDP, BDD
- Measures obtained using FTA in SHARPE
  - Reliability/availability, MTTF, importance measures, min-cuts, min-paths, product form CDFs

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